

# Textured Dreams

Nicholas Markle  
CS 4204 Final Project



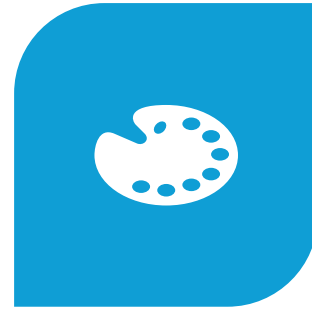
# What did I do



MY FINAL PROJECT WAS TO  
IMPLEMENT UVS INTO THE  
EXISTING GRAPHICS PIPELINE



UVS ARE 2D COORDINATES  
USED TO MAP A 3D MODEL'S  
SURFACE TO A 2D TEXTURE



DEFINE HOW TEXTURES ARE  
WRAPPED AROUND THE  
MODEL.



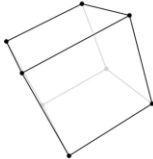
LEARNED HOW TO IMPLEMENT  
FROM THE LECTURE SLIDES AND  
KEENAN CRANE'S VIDEO.

# What are UVs

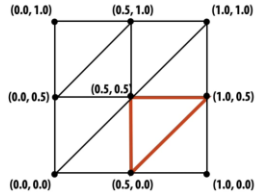
## Texture coordinates

- "Texture coordinates" define a mapping from surface coordinates to points in texture domain
- Often defined by linearly interpolating texture coordinates at triangle vertices

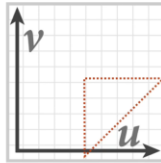
example: texture this cube



Suppose each cube face is split into eight triangles, with texture coordinates (u,v) at each vertex

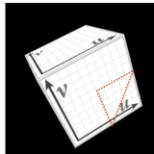


A texture on the [0,1]^2 domain can be specified by a 2048x2048 image



(location of highlighted triangle in texture space shown in red)

Linearly interpolating texture coordinates & "looking up" color in texture gives this image:



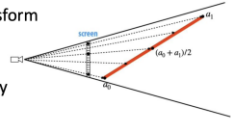
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## Texture Perspective

Project Point (perspective)

Due to perspective projection (homogeneous divide), barycentric interpolation of values on a triangle with different depths is not an affine function of screen XY coordinates

1. Apply Inverse of Camera Transform
2. Apply P
3. Divide by last element to apply perspective scaling
4. Apply O



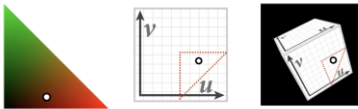
Homogenous Coordinate (W)

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## Texture Sampling 101

■ Basic algorithm for texture mapping:

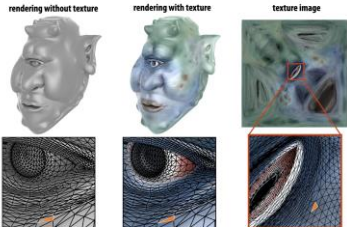
- for each pixel in the rasterized image:
  - interpolate (u, v) coordinates across triangle
  - sample (evaluate) texture at interpolated (u, v)
  - set color of fragment to sampled texture value



...sadly not this easy in general!

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## Texture mapping adds detail



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## Texture Perspective

■ Goal: interpolate some attribute  $\phi$  at vertices

- Basic recipe:
  - Compute depth z at each vertex
  - Evaluate Z := 1/z and P :=  $\phi/z$  at each vertex
  - Interpolate Z and P using standard (2D) barycentric coords
  - At each fragment, divide interpolated P by interpolated Z to get final value

$$w = \frac{n \cdot f}{f + n - p'' \cdot z}$$



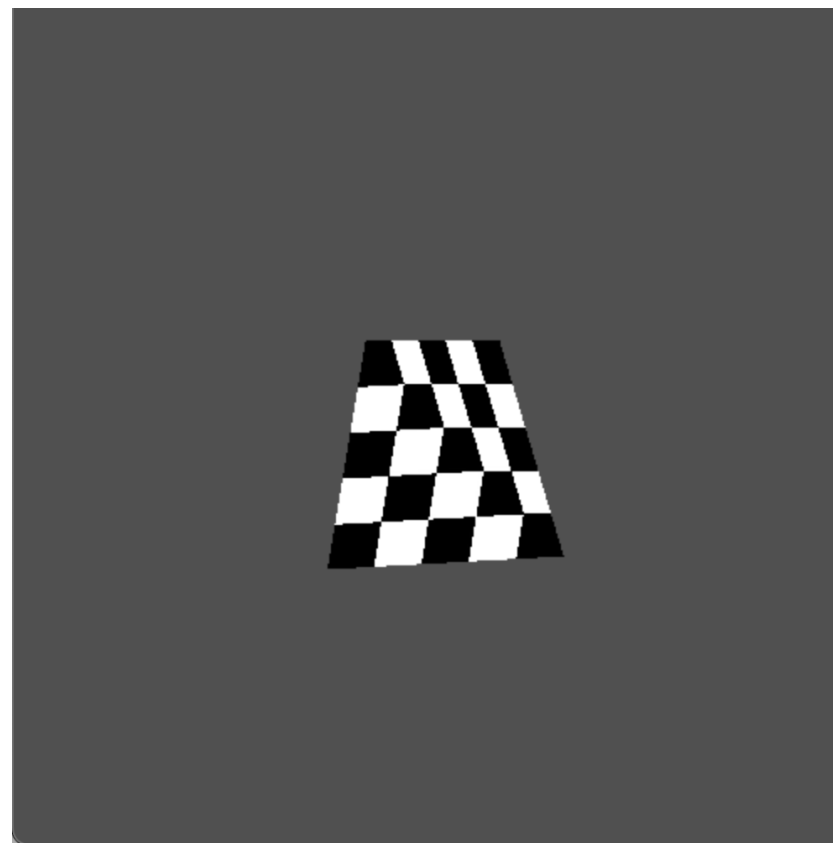
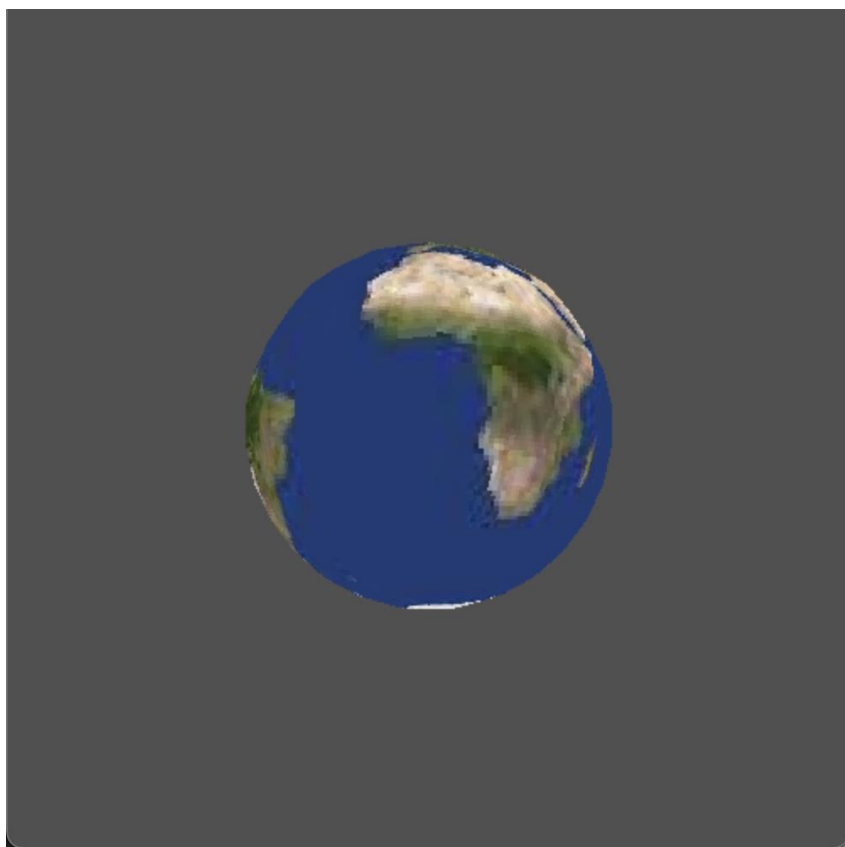
© derivation, see Lim, "Perspective-Correct Interpolation"

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# Affine implementation

- **Barycentric Coordinates:** Calculate the texture coordinates ( $u$  and  $v$ ) for the pixel using barycentric interpolation ( $\alpha$ ,  $\beta$ ,  $\gamma$ ) based on the triangle's vertices.
- **Clamping:** Ensure  $u$  and  $v$  are within the valid texture bounds (0 to 1)  
**Texture Sampling:** Sample the texture at the computed coordinates ( $u$ ,  $v$ ) and assign the resulting color to the image buffer.
- **Depth:** Update the depth buffer with the interpolated depth value ( $z_{\text{interpolated}}$ ).

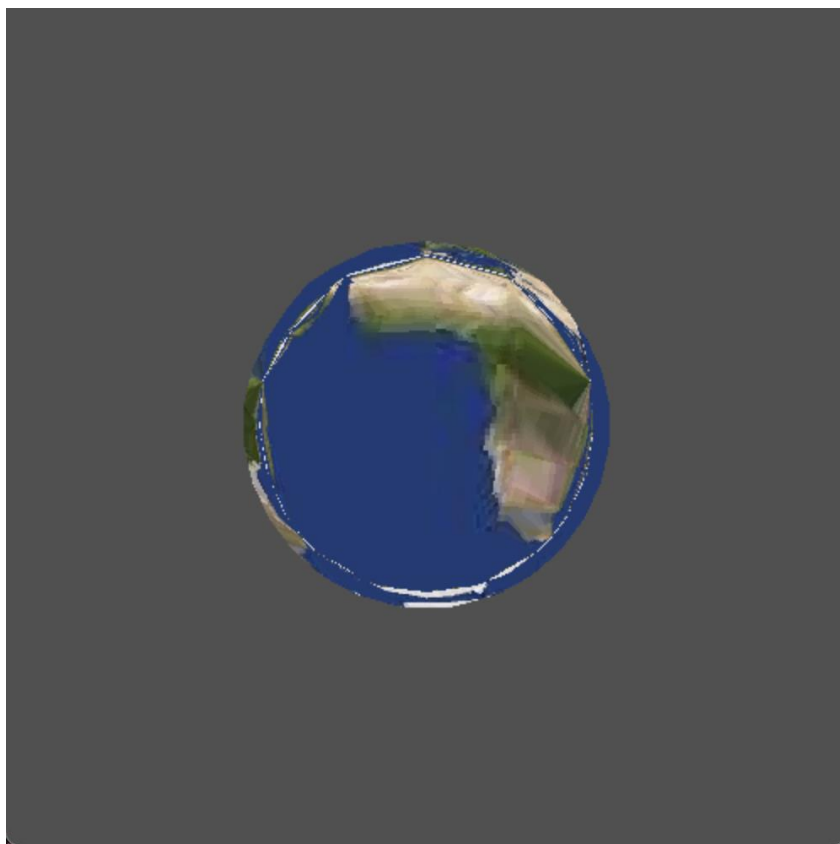
# Output from running Affine Implementation



# Perspective Correct Implementation

- **Inverse Depths:** Calculate the inverse of the depth values ( $1/z_0$ ,  $1/z_1$ ,  $1/z_2$ ) for each triangle vertex.
- **Depth Correction:** Adjust the barycentric coordinates ( $\alpha$ ,  $\beta$ ,  $\gamma$ ) using the inverse depth values to handle perspective correction ( $\alpha_w$ ,  $\beta_w$ ,  $\gamma_w$ ).
- **Normalization:** Normalize the corrected weights ( $\alpha_w$ ,  $\beta_w$ ,  $\gamma_w$ ).
- **Perspective-Correct UV Calculation:** Compute the corrected texture coordinates ( $u$ ,  $v$ ) by weighting the UVs of each vertex based on the perspective-corrected barycentric coordinates.
- **Clamping:** Ensure the corrected texture coordinates are within valid bounds (0 to 1).
- **Texture Sampling:** Sample the texture at the corrected coordinates and assign the resulting color to the image buffer.
- **Depth:** Update the depth buffer with the interpolated depth value ( $z_{\text{interpolated}}$ ).

Didn't quite get this working



## Final Remarks

Affine Implementation  
worked well

Perspective Correct  
Implementation is a bit buggy

Wish I hadn't been sick so  
much this semester